THE ROLE OF REGIONAL INTERACTION IN REGIONAL GROWTH: Competition and Complementarity in the U.S. Regional System

Geoffrey J.D. Hewings
Regional Economics Applications Laboratory, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA.

Michael Sonis
Regional Economics Applications Laboratory, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA and Bar Ilan University, Israel.

Federico A. Cuello
Regional Economics Applications Laboratory, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA and UNDP, Santo Domingo, Dominican Republic.

Faycal Mansouri
Faculté des Sciences Economiques et de Gestion de Tunis, Université de Tunis.

ABSTRACT The role of regional interaction in multi-regional growth is examined by estimating the parameters for a discrete nonlinear model of relative dynamics with maximum likelihood methods. This model specification approaches the issues of spatial dependence in a different form from the methods that have been used to date. It provides evidence for the view of multi-regional growth as a zero-sum game, in which a mixed pattern of competition and complementarity exists among non-contiguous regions. The approach is illustrated with an aggregate set of regions for the U.S. economy and forecasts are made of the progress of regional convergence into the next century. It is suggested the methodology might prove to be a useful alternative to the usual method of incorporating exogenous changes into regional models.

II. INTRODUCTION

Do regions compete or complement each other? Can these types of regional interactions coexist in a national economy? If so, do they fulfill the “first law of geography” in relation to the effects of neighbourhood or close spatial association? New approaches may be needed to address these questions. This paper examines one new model proposed recently by Dendrinos and Sonis (1990) for modelling the time-interaction of a single statistical population over multiple locations. It is applied to

The detailed comments and suggestions of Peter Dixon and the referees are very much appreciated.
an examination of the role of regional interaction in the growth of the U. S. regions. The parameters are obtained by classical maximum likelihood estimation of a log-linear specification; furthermore, the parameter signs and significance can be interpreted as characterizing the regional patterns of competition and complementarity.

The stimulus for this work was provided by increasing dissatisfaction with the way in which traditional econometric, input-output and linked models incorporate exogenous change into a specific regional model. For example, a typical econometric model for a region would use a national econometric ‘driver’; however, for many sectors of the Chicago regional economy, the linkages are far stronger with specific parts of the U. S. with the result that a great deal of potential explanation is lost when the exogenous data are specified for the U. S. as a whole rather than for specific subsets. When considering these issues with reference to Chicago (or any other region), a set of questions may be raised:

- **How does the region’s degree of self-sufficiency compare with other regions in the U. S. (and, for that matter, in the rest of the world)?**
- **Given the degree of interaction with the rest of the U. S., which parts of the external-to-region world within U. S. borders benefit the most from this interaction?**
- **What pattern of regional interaction emerges when the system of North American regional economies are considered? What implications does this pose for Chicago, in the context of the North American Free Trade Area?**
- **How can this information be used to better understand the nature of interregional trade in the U. S. and to provide more accurate forecasting systems for regional economies?**

The transformations that continue to evolve in the U. S. economy have modified significantly the nature and distribution of economic activity. Disparities in per-capita incomes (Amos, 1988), differences in the patterns of regional specialization, and organizational and technological changes at the firm level are all facts that call for a new approach to examine the way in which national economies function. As recent research suggests, the dominant trends of national growth are often not at all representative of the fluctuations taking place at the regional (sub-national) level in the U. S. These questions provide the major motivation for the present paper; the work of Henderson and Krueger (1965) provided some initial stimulation in that their forecasting and impact model for the Upper Midwest divided the external-to-the-region world into a nine-fold partition, providing the capability for each external region to exert a different influence upon the Upper Midwest.

The major objective is to provide an empirically based and tested framework for understanding spatial interactions among U.S. regions, so that the structural changes taking place in these interactions can be examined. In addition, this framework can be used in enhancing the predictive ability of regional econometric/input-output models of the kind represented by the Chicago Region Econometric Input-Output
The Role of Regional Interaction in Regional Growth

**Figure 1a. Existing System**

**Figure 1b. Proposed System**

**Model (CREIM)**. At the present time, most regional models exemplify the characterization of Bolton (1985) as ‘top-down’ (see Figure 1a). Essentially, they are ‘two-region’ models: the region of interest and the nation. The goal of this research is to build an alternative framework; here, the nation is replaced by a space-time system for a finite division of the U. S. economy into individual states or census regions (see Figure 1b).

With such a specification, it is hoped that the richness of our understanding of spatial interaction and interdependencies can be harnessed for the provision of more sensitive modelling and forecasting of individual regions. The approach chosen is still parsimonious in model scope and certainly avoids any tendency towards data avaricious models whose grand design hides the impossibility of their empirical implementation.

As a by-product of this research, it is hoped that a better understanding of the nature of the space-time regional economic system in the U. S. will be revealed. Opportunities to provide the basis for a set of taxonomies of regional economy-types, for growth and development trajectories or a series of stylized facts in the tradition of Johansen (1960) and Chenery and Syrquin (1975) could be explored.

**2. ANTECEDENTS**

Econometric modelling of space-time processes requires dealing with the problem of spatial effects. These effects are known as spatial heterogeneity (heteroskedasticity) and spatial dependence (autocorrelation). The various methods devised for dealing with these problems involve the use of a matrix of weights describing regional contiguity patterns or network linkages. This scheme underlies the three models of spatial econometrics: weighted OLS, GLS and Spatial Seemingly-Unrelated Regression (SSUR).

---

2 CREIM was developed in cooperation with Richard Conway whose Washington State projection and Simulation Model (Conway, 1979, 1990, 1991) has been in use for many years.
Use of the weight matrix stems from the acceptance of the first law of geography, whereby there would be an expectation of observing a greater correlation between series describing processes in regions that are closer in space. But nothing guarantees that the interactions picked by the weight matrix represent the complete set of significant links between the regions studied that are influenced by spatial effects. This is one of the major research challenges in the spatial econometrics literature (Anselin, 1988, p. 254). A model specification that is free from the explicit incorporation of these effects would contribute to the liberation of the econometric modelling of space-time processes from using these techniques, while addressing adequately the research questions formulated in Section 1.3.

The traditional views on regional growth (Richardson, 1978, pp. 145-146) state that growth in regional output is either (a) a zero-sum game, and thus growth in a region can take place only in expense of growth in another region, or (b) generative, implying that an efficient organization of production within each region will lead to increased regional and national growth in output. In the first case, regional interaction plays a fundamental role in determining regional growth and it is possible to find a mixed pattern of regional competition and complementarity. In the second case, regional growth seems to be determined also by processes endogenous to the region.

These views may be reconciled if empirical work is able to show that it is how the dynamics of sectoral interactions within the regions react to the regional interaction with other regions that determine the patterns of competition and complementarity in the multi-regional system. This paper examines only the last part of this hypothesis, to explore if indeed there exists a pattern of regional interaction with a specific econometric structure. Further work will be needed in (a) a multiple time series framework and (b) a multisectoral specification to examine the role of the sectoral dynamics internal to regions in determining the observed patterns of regional interaction.

3. DISCRETE RELATIVE NONLINEAR DYNAMICS

Let $\Gamma_{ST}$ be an economy defined over space and time. The indices $S$ and $T$ indicate the finite number of regions in the economy and a finite time horizon respectively. Regional economic activity within the nation is represented by an $S$-dimensional vector $X_t = (X_{1t}, X_{2t}, \ldots, X_{St})$, $[0 < X_{st} < 1; s = 1, \ldots, S; t = 1, \ldots, T]$. Given the data available, this vector is defined as a vector of Gross Regional Products (GRPs), at constant prices of 1982.

The main issue centres on the most efficient way to examine the pattern of regional interaction in the context of the global (national) dynamics of $\Gamma_{ST}$. To answer this question, the behaviour of the GRP stocks needs to be studied by expressing their values relative to GNP:

---

3 However, as one of the reviewers has correctly pointed out, there is no guarantee that spatial dependence will be eliminated by expressing variables with respect to a numeraire; the empirical problem is the degree to which this process affects dependence. Is it merely a re-scaling process or one that incorporates other properties?
The Role of Regional Interaction in Regional Growth

\[ Y_{st} = \frac{1}{\sum_s X_{st}} \]  
\[ \quad [0 < Y_{st} < 1; s = 1, ..., S; t = 1, ..., T] \]  
\[ \text{(1)} \]

where \( X_{st}, Y_{st} \) are the absolute and relative values of gross national product in region \( s \) at time period \( t \).

The D-S model (after Dendrinos and Sonis, 1990) represents these relative dynamics as a discrete nonlinear process of the form:

\[ Y_{1r+1} = \frac{1}{1 + \sum_j F_{jt}} F_{jr} \quad [j = 2, 3, ..., S] \]  
\[ \text{(2)} \]

\[ Y_{sr+1} = \frac{F_{sr}}{1 + \sum_j F_{jt}} \quad [j = 2, 3, ..., S] \]

Here \( \sum_s Y_{st} = 1 \) \( [s = 1, 2, ..., S] \)

and \( \frac{Y_{st+1}}{Y_{1r+1}} = F_{st} \) \( [s = 2, 3, ..., S] \)

i.e. the first region is considered as a numeraire (reference) region. The regions are ranked by their shares of national GNP in order to make the choice of the numeraire region; it was decided to use the region with the smallest share of GNP, the Rocky Mountain region, as the numeraire. In this study the log-linear specification of the function \( F_{st} \) will be used. Dendrinos and Sonis (1990) define this function as:

\[ F_{st} = A_s \prod_k Y_{kr}^{a_{sk}} \quad [F_{st} > 0; s = 2, ..., S; k = 1, ..., S] \]  
\[ \text{(3)} \]

where \( A_s > 0 \) represents the locational advantages of all regions \( s \in S \) and:

\[ a_{sk} = \frac{\partial \ln F_{st}}{\partial \ln Y_{kr}} \quad [s = 2, 3, ..., S; k = 1, 2, ..., S] \]  
\[ \text{(4)} \]

are the interregional growth elasticities, with \( -\infty < a_{sk} < \infty \).

In log-linear form, (2) and (3) can be written as:

\[ \ln Y_{sr+1} - \ln Y_{1r+1} = \ln A_s + \sum_{k=1}^{s} a_{sk} \ln Y_{kr} \quad [s = 2, ..., S; t = 1, ..., T] \]  
\[ \text{(5)} \]

At this level of aggregation, regional interaction is dominated by the pursuit of each region’s increase in its share of GNP, which is accomplished by improving their comparative advantages. This improvement depends upon the behaviour of the rest
of the regions, which is taken into account by the sign and value of each \( a_{ik} \) (composite growth elasticities), given the locational comparative advantage factor \( A_k \). Negative composite elasticities would identify competing regions and positive elasticities would identify complementary regions. Existence of both types of interaction would be evidence for the interpretation of regional growth as a zero-sum game, in which growth in any \( y_i \) would be in expense of the growth of at least one other \( y_j (j \neq i) \) in \( \Gamma_{ST} \).

Predictions of the level of the regions' GRPs are obtained by multiplying \( Y_{ri} \) by corresponding forecasts of the Gross National Product (obtained from exogenous sources). These forecasts are expected to reveal the (bounded) cyclical deviations from the GRPs from the dominant trend of GNP growth, for the discrete map of relative nonlinear dynamics has been shown to display several different types of dynamics, including stability, periodicity and chaos (cf. Dendrinos and Sonis, 1990: Part III). Given the limited time series available, it would not be possible to extend this analytical framework to the complete set of U.S. states; in this case, some of the ideas and methods that exploit notions of hierarchy and feedback loops would need to be considered (see Sonis, Gazel and Hewings, 1995). A similar problem was faced by White and Hewings (1982) in applying spatial seemingly unrelated regression analysis to modelling employment within a multiregional context within a state.

4. **MAXIMUM LIKELIHOOD ESTIMATION**

The transformations performed to the series of GRPs as required by the specification of the D-S model determine that its parameterisation is free from spatial effects or other sources of structural instability. In particular, (a) the model is free from the influence of the global process of GNP growth, as the series have been deflated by GNP when expressed in relative terms, and (b) the model does not specify an \( a \) priori expectation about spatial heterogeneity and dependence. In essence, the model explores the degree to which the regions interact through their competition for relative shares of GNP. It is not clear whether such a process avoids the problem of spatial dependence or incorporates it explicitly through the procedure of choosing a region of reference (numeraire) in equations 3 and 5. If this is the case, the pattern of regional interaction can emerge from estimation of the D-S model without using a weight matrix.

Rewriting the rows of equation (5) in matrix form:

\[
y_j = X\beta_j + e_j \quad j = 2, ..., S
\]

where:

\[
y_j = \begin{bmatrix}
\ln Y_{j1} - \ln Y_{11} \\
\vdots \\
\ln Y_{jT} - \ln Y_{1T}
\end{bmatrix}
\]

\[
X = \begin{bmatrix}
\ln Y_{12} - \ln Y_{12} \\
\vdots \\
\ln Y_{1(T-1)} - \ln Y_{1(T-1)}
\end{bmatrix}
\]

\[
e_j = \begin{bmatrix}
e_{j1} \\
\vdots \\
e_{jS}
\end{bmatrix}
\]
The Role of Regional Interaction in Regional Growth

\[
X = \begin{bmatrix}
1 & \ln Y_{11} & \ln Y_{21} & \cdots & \ln Y_{s1} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
1 & \ln Y_{1t} & \ln Y_{2t} & \cdots & \ln Y_{st} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
1 & \ln Y_{1T-1} & \ln Y_{2T-1} & \cdots & \ln Y_{sT-1} \end{bmatrix}_{(T-1) \times (S+1)}
\]

\[
\beta_j = \begin{bmatrix}
\ln A_j \\
a_{j1} \\
\vdots \\
a_{js} \end{bmatrix}_{(S+1) \times 1}
\]

provides the elements for its maximum likelihood (ML) estimation. Standard references (such as Cramér, 1986; Judge et al., 1988) provide the formulation of the ML estimator for the normal case. Estimation of the log-linear D-S model requires that a log-normal distribution be used; details are provided in an appendix.

In specifying the model, important issues related to misspecification (due to simultaneity) were not addressed explicitly although several alternative forms of the equations were tried. By adopting a relative dynamics view of the processes of change, it is hoped that some of these problems can be minimised. The results suggest that these problems are neither trivial nor easy to accommodate.

5. EMPIRICAL RESULTS

Charts 1 through 8 provide some background perspective about the behaviour of the macro (census) regions over the period 1964 through 1988. Two variables are plotted on each chart, the rate of growth of gross regional product and the growth of the regional share of gross national product. These charts should be read in comparison to the summary information provided in Chart 9. Here, the regional shares of gross national product have been displayed for the same time period. During this period, the Great Lakes region experienced a decrease in its share of national product even though, during much of the period, the rate of growth of regional product was positive. Obviously, this region's performance was outstripped by other regions such as the Southeast. Note also the varying degrees to which the recessions of the early 1970s and 1980s affected regional performance. The Southeast and Southwest experience only one negative growth rate in GRP in 1980s while the Great Lakes region had three years with negative growth rates. However Chart 9 provides no information on the relationships between the regions and it is in Table 1 that these relationships are explored.

Table 1 summarizes the parameter values obtained from fitting the D-S model to the logarithm of the series of U.S. GRPs relative to the U.S. GNP. A pattern of regional interaction has emerged that links non-contiguous regions. This confirms the concern expressed in Section 1 on the generality of the first law of geography.
RATE OF GROWTH OF GROSS REGIONAL PRODUCT VS. RATE OF GROWTH OF THE REGIONAL SHARE OF GNP.

Chart 2. Mid East Census Region of the U.S., 1963-1989:
RATE OF GROWTH OF GROSS REGIONAL PRODUCT VS. RATE OF GROWTH OF THE REGIONAL SHARE OF GNP.

RATE OF GROWTH OF GROSS REGIONAL PRODUCT VS. RATE OF GROWTH OF THE REGIONAL SHARE OF GNP.
The Role of Regional Interaction in Regional Growth

RATE OF GROWTH OF GROSS REGIONAL PRODUCT VS. RATE OF GROWTH OF THE REGIONAL SHARE OF GNP.

Chart 5. Southeast Census Region of the U.S., 1963-1989:
RATE OF GROWTH OF GROSS REGIONAL PRODUCT VS. RATE OF GROWTH OF THE REGIONAL SHARE OF GNP.

RATE OF GROWTH OF GROSS REGIONAL PRODUCT VS. RATE OF GROWTH OF THE REGIONAL SHARE OF GNP.
Table 1. Regression Results of Log-Linear Space-Time Model of Relative Dynamics

<table>
<thead>
<tr>
<th>Region</th>
<th>New England</th>
<th>Mid East</th>
<th>Great Lakes</th>
<th>Great Plains</th>
<th>South East</th>
<th>South West</th>
<th>Rocky Mountain</th>
<th>Far West</th>
<th>Constant</th>
<th>R² Adj</th>
<th>Durbin-Watson</th>
</tr>
</thead>
<tbody>
<tr>
<td>New England</td>
<td>0.5202</td>
<td>-2.1077</td>
<td>-2.5073</td>
<td>0.1139</td>
<td>-2.2878</td>
<td>-1.0491</td>
<td>-1.3317</td>
<td>-1.3812</td>
<td>-18.5500</td>
<td>0.9616</td>
<td>1.5846</td>
</tr>
<tr>
<td>(t-ratios)</td>
<td>(-0.4319)</td>
<td>(-0.9906)</td>
<td>(-1.1292)</td>
<td>(-0.1030)</td>
<td>(-1.1810)</td>
<td>(-0.8275)</td>
<td>(-2.2148)</td>
<td>(-0.8761)</td>
<td>(-0.8037)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mid East</td>
<td>0.4553</td>
<td>-0.1906</td>
<td>-1.2312</td>
<td>0.6915</td>
<td>-1.3464</td>
<td>-0.2565</td>
<td>-1.2054</td>
<td>-0.7167</td>
<td>0.0033</td>
<td>0.9889</td>
<td>1.8890</td>
</tr>
<tr>
<td>(t-ratios)</td>
<td>(-0.5815)</td>
<td>(-0.1491)</td>
<td>(-0.9102)</td>
<td>(-0.8742)</td>
<td>(-1.1738)</td>
<td>(-0.3183)</td>
<td>(-3.2986)</td>
<td>(-0.7593)</td>
<td>(-0.3991)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Great Lakes</td>
<td>0.8561</td>
<td>3.3855</td>
<td>2.4885</td>
<td>1.1644</td>
<td>1.6012</td>
<td>1.0678</td>
<td>-0.2229</td>
<td>2.4901</td>
<td>25.9310</td>
<td>0.9793</td>
<td>2.1895</td>
</tr>
<tr>
<td>(t-ratios)</td>
<td>(-0.6557)</td>
<td>(-1.5590)</td>
<td>(-1.0779)</td>
<td>(-1.0784)</td>
<td>(-0.8484)</td>
<td>(-0.7715)</td>
<td>(-0.3666)</td>
<td>(-1.5362)</td>
<td>(-1.0907)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Plains</td>
<td>0.1754</td>
<td>0.1774</td>
<td>-0.0071</td>
<td>0.2049</td>
<td>-0.4749</td>
<td>-0.0486</td>
<td>-0.5518</td>
<td>-0.0049</td>
<td>0.5555</td>
<td>0.9775</td>
<td>1.8684</td>
</tr>
<tr>
<td>(t-ratios)</td>
<td>(-0.2484)</td>
<td>(-0.1539)</td>
<td>(-0.0059)</td>
<td>(-0.2872)</td>
<td>(-0.4591)</td>
<td>(-0.0669)</td>
<td>(-1.6744)</td>
<td>(-0.0057)</td>
<td>(-0.0456)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>South East</td>
<td>-0.1435</td>
<td>0.3142</td>
<td>-0.6930</td>
<td>0.0553</td>
<td>0.3166</td>
<td>-0.2077</td>
<td>-0.8081</td>
<td>0.3099</td>
<td>-1.2271</td>
<td>0.9469</td>
<td>2.0281</td>
</tr>
<tr>
<td>(t-ratios)</td>
<td>(-0.2047)</td>
<td>(-0.2700)</td>
<td>(-0.5610)</td>
<td>(-0.0988)</td>
<td>(-0.3178)</td>
<td>(-0.2784)</td>
<td>(-2.4926)</td>
<td>(-0.3559)</td>
<td>(-0.0966)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>South West</td>
<td>-0.7915</td>
<td>-1.0595</td>
<td>-1.4161</td>
<td>-0.2589</td>
<td>-1.1060</td>
<td>0.0206</td>
<td>-1.1448</td>
<td>-0.5933</td>
<td>0.0000</td>
<td>0.6736</td>
<td>1.9996</td>
</tr>
<tr>
<td>(t-ratios)</td>
<td>(-1.2197)</td>
<td>(-0.9999)</td>
<td>(-1.2630)</td>
<td>(-0.3948)</td>
<td>(-1.1632)</td>
<td>(-0.0309)</td>
<td>(-3.7794)</td>
<td>(-0.7584)</td>
<td>(-1.0713)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Far West</td>
<td>1.4530</td>
<td>1.1348</td>
<td>1.3743</td>
<td>1.0800</td>
<td>1.3111</td>
<td>0.4859</td>
<td>-0.2264</td>
<td>1.7041</td>
<td>18.4780</td>
<td>0.9540</td>
<td>1.9152</td>
</tr>
<tr>
<td>(t-ratios)</td>
<td>(-1.8260)</td>
<td>(-0.8565)</td>
<td>(-0.9768)</td>
<td>(-1.5815)</td>
<td>(-1.1280)</td>
<td>(-0.5786)</td>
<td>(-0.6068)</td>
<td>(-1.7296)</td>
<td>(-1.2708)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Note: Numeraires of dependent variable: Rocky Mountain.
This indicates that given (a) the absence of spatial heterogeneity or dependence, (b) developed transport and communications networks, and (c) the differences in the patterns of regional specialization, use of regional contiguity patterns would provide an incomplete picture of the extent of the interdependence with regions other than the nearest neighbours. While not all the variables are statistically significant, the relationships provide some indications of the direction of the interactions. Table 2 provides a qualitative interpretation of the results; the formal relationships have been reduced to signs and, in the second part of the table, a suggested hierarchy of relationships is proposed on a complementarity-competition scale. The Great Lakes (GL) and Far West (FW) regions exert strong complementarity relationships with the rest of the states but the relationship of the other states with these regions is predominantly negative. For the other regions, the relationships are more varied. However, the relationships would be consistent with a priori expectations; the regions that are dominant producers of intermediate goods and services seem to be positively linked with other regions. The next stage in the investigation would be to explore the components of gross national product and sectoral disaggregation; it is at this, more detailed level, that greater insights into the nature of the relationships will be revealed.

The previous points are more pertinent when the highly asymmetric nature of the econometric structure uncovered is noticed. This is evidenced by some regions' competition as suppliers to other regions while complemented by the same regions when demanding from them. This is sufficient evidence for the existence of a simultaneous pattern of competition and complementarity among the U.S. regions. It implies that policies affecting positively the growth of specific regions' share of GNP will increase or decrease the corresponding dependent region's share of GNP according to the competitive or complementary relationship between them, as indicated by the sign of the corresponding growth elasticities. However, many of the individual coefficient estimates would not survive rigorous t-test conditions for their significance; as a result, the analysis must be presented as a first experiment rather than the basis for conjecture about the exact nature of interdependencies across space. However, the results presented here complement those of Sonis, Gazel and Hewings (1995) in the context of an examination of the feedback effects generated by interregional trade. These results become even more important when consideration of the nature of external-to-the-U.S. linkages of these regions are taken into account; for example, the Great Lakes, Far West and Mid East regions export between 40-50% of their international exports to Canada, Asia and Europe respectively. These external linkages portend a degree of interdependence with the world economy that would produce a complex web of intra-U.S. interdependencies of the kind suggested by Table 1.

Charts 10 and 11 indicate that, in effect, the model is able to predict the bounded fluctuations of the cyclical changes in the growth of the regional shares, just as was observed during the period (1963-89) and displayed in Chart 12. Note that the vertical axis of Chart 10 shows the rates of growth of the shares, not the absolute changes in the share values. Chart 11 highlights three regions that appear to be very interdependent; even here, the rates of growth of the predicted shares are out of phase through 2020. It seems that in the long run, the regional shares will converge to a steady state level fairly close to the predictions of the model. In addition, the accuracy of the predicted
Table 2. Qualitative Analysis of the Competitive/Complementary Relationships

(a) Qualitative Relationships

<table>
<thead>
<tr>
<th></th>
<th>NE</th>
<th>ME</th>
<th>GL</th>
<th>GP</th>
<th>SE</th>
<th>SW</th>
<th>RM</th>
<th>FW</th>
<th>+</th>
<th>-</th>
</tr>
</thead>
<tbody>
<tr>
<td>NE</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2</td>
<td>6</td>
</tr>
<tr>
<td>ME</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2</td>
<td>6</td>
</tr>
<tr>
<td>GL</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>7</td>
<td>1</td>
</tr>
<tr>
<td>GP</td>
<td>+</td>
<td>+</td>
<td>-</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>3</td>
<td>5</td>
</tr>
<tr>
<td>SE</td>
<td>-</td>
<td>+</td>
<td>-</td>
<td>+</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>4</td>
<td>5</td>
</tr>
<tr>
<td>SW</td>
<td>-</td>
<td>-</td>
<td>+</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>1</td>
<td>7</td>
</tr>
<tr>
<td>FW</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>7</td>
<td>1</td>
</tr>
<tr>
<td>+</td>
<td>5</td>
<td>4</td>
<td>2</td>
<td>6</td>
<td>3</td>
<td>3</td>
<td>0</td>
<td>3</td>
<td>7</td>
<td>4</td>
</tr>
<tr>
<td>-</td>
<td>1</td>
<td>3</td>
<td>5</td>
<td>1</td>
<td>4</td>
<td>4</td>
<td>7</td>
<td>4</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

(b) Qualitative ordering

<table>
<thead>
<tr>
<th></th>
<th>GP</th>
<th>NE</th>
<th>ME</th>
<th>SE</th>
<th>SW</th>
<th>FW</th>
<th>GL</th>
<th>RM</th>
</tr>
</thead>
<tbody>
<tr>
<td>GL</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>-</td>
</tr>
<tr>
<td>FW</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>-</td>
</tr>
<tr>
<td>SE</td>
<td>+</td>
<td>-</td>
<td>+</td>
<td>+</td>
<td>-</td>
<td>+</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>GP</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>NE</td>
<td>+</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>ME</td>
<td>+</td>
<td>+</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>SW</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>+</td>
<td>-</td>
<td>+</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

Regional shares can be assessed from Chart 12, which presents the percent deviation of the predicted from the observed regional shares. There is some suggestion that the model's deviations from observed shares has increased over the observed time period even though the forecasts (Chart 10) indicate convergence. Until a longer time series of data is available, it will be difficult to know whether the dampening process implied in Chart 10 is indicative of a real convergence towards stable shares. The experience of the 1990s recession suggests that U.S. macro regions are still not marching in lock-step with the nation; however, the major concern is whether this is a short-term deviation from a longer-term trend towards convergence of behaviour. Note, also, that the cyclical behaviour (Chart 11) for three regions still suggests considerable differences in the growth rates for the shares in terms of timing and amplitude for the period 1987 through 2020 before a significant dampening-out process begins. In the historical period (Chart 12), the year-to-year fluctuations are far more varied than during the forecast period since the D-S model tends to smooth out fluctuations.

6. CONCLUSIONS AND DIRECTIONS FOR FURTHER WORK

This paper has uncovered an asymmetric pattern of competition and complementarity among the U.S. regions, using a nonlinear dynamic functional form that is endogenised...
the spatial interaction effects and that reveals bounded cycles of fluctuating growth over time. The results presented in Charts 10 and 11 point clearly towards the significance of the lag structure over space and time among the U.S. regions in a multiple auto-regressive moving-average (ARMA) framework. Another important step in this research is to provide an empirical explanation for the patterns of competition and complementarity uncovered here. This can be accomplished by moving from the macro level of this paper to the meso level, i.e. by estimating the D-S model with the series of regional sectoral outputs, in order to determine what elements in the interactions among the sectoral production of regions determine the relationships at the macro level found in this paper.

Moreover, further work follows from the contradictions between the assumptions underlying the ML estimator derived and those of the D-S model, which carries two fundamental assumptions: relativity and interdependence. Relativity means that the model is predicting the dynamics of GRPs relative to the global dynamics of the national economy, based on a sample of non-experimental data. Classical econometrics' asymptotic results for parameter estimation assuming a repeated-sampling data-generating process are not quite adequate for the characteristics of the sample. Second, the issue of interdependence clashes directly with the assumption of independence of classical econometrics. Additional research should tackle this contradiction by deriving an appropriate Bayesian estimator for the D-S model, departing from Lindley and Smith's (1972) results on the exchangeability of the linear Bayesian model.

Returning to the issues raised in the Introduction of this paper, it would seem that some useful insights could be gained from the placement of a 'filter' between national-level changes and their impacts on a specific region. Further empirical analysis and experimentation will have to be performed to help shape the specific form of this filter. During this experimentation, it will be important to incorporate detailed specification of linkages between sectors (through transformations of input-output type relationships) and thus move the modelling system closer to one in which a more complete vision of space-time-sectoral interdependencies is portrayed. However, the system described in this presentation requires, for efficient estimation purposes, that the time dimension exceeds the spatial dimension; the limited reach of the time series will preclude applications of the analysis to a system of all fifty states. For such an application to take place, some form of hierarchical procedure will have to be employed creating additional conceptual and empirical problems about the ways in which spatial dependence are addressed.

REFERENCES


APPENDIX

Estimation of the log-linear Dendrinos-Sonis model requires that a log-normal distribution be used. For each region $j$, the joint log-normal density function of the sample of relative population components and the unknown parameters $\beta_j$ and $\sigma_j^2$ can be expressed as a likelihood function of the form:

$$
\ln L(\beta_j, \sigma_j^2; y_j, X) = -\left(\frac{T-1}{2}\right) \ln (2\pi) - \left(\frac{T-1}{2}\right) \ln (\sigma_j^2) - \frac{(y_j - X\beta_j)'(y_j - X\beta_j)}{2\sigma_j^2} \tag{A.1}
$$

Maximization of this likelihood function occurs for the value of the vector $\beta_j$ that yields the larger probability for the realizations of the observations, $y_j$. Taking the partial derivative of (A.1) with respect to $y_j$ and setting it equal to zero yields the efficient, consistent and best unbiased maximum likelihood estimator (Judge et al.,
1988, pp. 223-229):

\[ \beta_j = [X'X]^{-1}X'y_j \quad \text{with} \quad \hat{\beta}_j = N(\beta_j, \sigma^2_j, [X'X]^{-1}) \]

Maximizing (A.1) with respect to \( \sigma^2_j \) yields the estimator, \( \hat{\sigma}^2_j \):

\[ \hat{\sigma}^2_j = \sigma^2_j \frac{(y_j - X\hat{\beta}_j)'(y_j - X\hat{\beta}_j)}{T - 1} \quad \text{with} \quad E(\hat{\sigma}^2_j) = \sigma^2_j \frac{(T - 1) - (S + 1)}{T - 1} \]  

which is biased since as \( T \to \infty \), \( \hat{\sigma}^2 \) does not converge to \( \sigma^2 \). Multiplication of (A.3) by \( T/[T - (S + 1)] \) transforms it into \( \hat{\sigma}^2 \), i.e., a consistent estimator of \( \sigma^2 \):

\[ \hat{\sigma}^2_j = \frac{(y_j - X\hat{\beta}_j)'(y_j - X\hat{\beta}_j)}{(T - 1) - (S + 1)} \]